

# Department of Mathematics (incl. Math. Statistics)

# **Syllabus**

for course at advanced level

Enumerative combinatorics
Enumerativ kombinatorik

7.5 Higher Education Credits
7.5 ECTS credits

 Course code:
 MM8018

 Valid from:
 Autumn 2019

 Date of approval:
 2009-11-23

 Changed:
 2009-11-23

Department Department of Mathematics (incl. Math. Statistics)

Main field: Mathematics/Applied Mathematics

Specialisation: AXX - Second cycle, in-depth level of the course cannot be classified

#### **Decision**

This syllabus has been approved by the Board of the Faculty of Science at Stockholm University on 23 November 2009. Technical revision by the Student Office 2019-04-25.

## Prerequisites and special admittance requirements

To qualify for the course knowledge equivalent to 90 credits in Mathematics is required, where Combinatorics II SL 7.5 credits is included. Also required is knowledge equivalent to Swedish upper secondary course English B or equivalent to one of the following tests. Cambridge CPE and CAE: Pass, IELTS: 6.0 (with no part of the test below 5.0), TOEFL (paper based): 550 (with minimum grade 4 on the written test part), TOEFL (computer based): 213, TOEFL (internet based): 79.

#### Course structure

**Examination code**Name
Higher Education Credits
F818
Enumerative combinatorics
7.5

#### Course content

The course covers basic methods of enumerative combinatorics. "The twelve- fold way", sieve methods, for example various examples of inclusion-exclusion, the involution principle and determinant methods to count lattice paths. Different aspects of the theory of partially ordered sets, for example lattice theory, Möbius inversion in posets and connections with topology.

#### Learning outcomes

It is expected that the student after taking the course will be able to

- define and prove properties of combinatorical standard objects and sequences of numbers
- reformulate and thereby solve combinatorical problems in terms of combinatorical standard objects
- do calculations and prove properties of formal power series
- prove recursions, generating functions and explicit expressions for combinatorically defined sequences
- construct combinatorical proofs of identities and inequalities
- use Möbius inversion, inclusion-exclusion and related sieve methods to solve enumerative problems
- define and prove properties of different classes of posets
- describe and perform calculations in the incidence algebra of a poset
- determine the Möbius function of posets with different methods and interpret them in topological terms

# **Education**

The education consists of lectures, exercises and submitted work.

### Forms of examination

a. Examination for the course is in the following manner: measurement of knowledge takes place through written and/or oral examination.

b. Grading is carried out according to a 7-point scale related to learning objectives:

A = Excellent

B = Very Good

C = Good

D = Satisfactory

E = Sufficient

Fx = Fail

F = Fail

- c. Grading criteria for the course will be distributed at the start of the course.
- d. A minimum grade of E is required to pass the course.
- e. Students who fail to achieve a pass grade in an ordinary examination have the right to take at least further four examinations, as long as the course is given. The term "examination" here is used to denote also other compulsory elements of the course. Students who have achieved a pass grade on an examination may not retake this examination in order to attempt to achieve a higher grade. Students who have failed to reach a pass grade on two occasions have the right to request that a different teacher be appointed to set the grade of the course. A request for such appointment must be sent to the departmental board.

#### Interim

Students may request that the examination is carried out in accordance with this syllabus even after it has ceased to apply. This right is limited, however, to a maximum of three occasions during a two-year-period after the end of giving the course. A request for such examination must be sent to the departmental board.

#### Misc

The course is a component in the master programs in mathematics and in applied mathematics, and it can also be taken as an individual course.

#### Required reading

Course literature is decided by the departmental board and is described in an appendix to the syllabus.