### This is a translation of the Swedish original Page 1/2

# Department of Mathematics (incl. Math. Statistics)

# Syllabus

# for course at advanced level Computability and constructive mathematics Beräkningsbarhet och konstruktiv matematik

Course code: Valid from: Date of approval: Department

Subject Specialisation: MM8026 Autumn 2011 2011-11-21 Department of Mathematics (incl. Math. Statistics)

Mathematics/Applied Mathematics AXX - Second cycle, in-depth level of the course cannot be classified

# Decision

This syllabus was approved by the Board of the Faculty of Science at Stockholm University 2011-11-21.

# Prerequisites and special admittance requirements

Admission to the course requires knowledge equivalent to at least 90 credits in mathematics. English B/English 6 or equivalent.

### Course structure

Examination code	Name
HELA	Computability and constructive mathematics

# Course content

The course covers fundamental constructibility issues in mathematics and gives an introduction to general constructive methods in mathematics.

Models for computations: Turing machines, register machines, lambda calculus. Universal machines and the halting problem. Rice's theorem. Relative computability. Undecidability in group theory and number theory. Computable real numbers and elementary constructive analysis. Specker sequences. Recursive realizability. The Brouwer-Heyting-Kolmogorov interpretation of logic. Constructive logic and some brief type theory.

### Learning outcomes

After taking the course, the student is expected to be able to:

- \* State and prove theorems on (un)decidability and apply them to problems in mathematics.
- \* Describe the theory of constructive proofs and apply it to some area of mathematics.

### Education

Instruction consists of lectures and exercises.

# Forms of examination

a. The course is examined as follows: Knowledge assessment takes the form of written assignments as well as written and oral exams.

b. Grades are assigned according to a seven-point goal-related grading scale:

A = Excellent



7.5 Higher Education

**Higher Education Credits** 

75

7.5 ECTS credits

Credits

B = Very Good C = Good D = Satisfactory E = Sufficient Fx = Fail (more work required before credit can be awarded) F = Total fail

c. The grading criteria will be distributed at the beginning of the course.

d. To be awarded a pass, a minimum of grade E is required.

e. Students who fail an ordinary examination are entitled to sit additional examinations as long as the course is offered. There is no restriction on the number of examinations. Examinations also include other obligatory elements of the course. Students who have passed an examination may not resit it in order to achieve a higher grade. Students who have failed on two occasions are entitled to request the appointment of a different examiner for the next examination. Any such request must be made to the departmental board. The course has at least two examinations for each academic year in the years in which instruction is provided. Intervening years include at least one examination.

f. A student who receives the grade Fx will be given an opportunity to upgrade to E by successfully completing some extra task(s) assigned by the examiner, who also decides on the criteria to be fulfilled in order to pass. The completion must take place before the following examination session.

### Interim

Students may request that the examination be conducted in accordance with this course plan even after it has ceased to be valid. However, this may not take place more than three times over a two year period after course instruction has ended. Requests must be made to the departmental board. The provision also applies in the case of revisions to the syllabus.

## Misc

This course is offered as part of the Master's Programme in Mathematics and as a separate course.

### **Required reading**

Course literature is decided by the departmental board and described thereafter in an appendix to the course plan.